

Chapter 14 / **Example 14****Goodness of fit to binomial distribution**

In a trial three coins are tossed.

- a** Find the probability of obtaining: 0 heads, exactly 1 head, exactly 2 heads, exactly 3 heads.

Hagar tosses three coins 200 times and makes a note of the number of heads each time. Her results are as follows.

Number of heads	Probability
0	28
1	67
2	83
3	22

She is interested to find out if her coins are fair and so performs a  $\chi^2$  goodness-of-fit test at the 5% significance level on her data.

- b** Use the probabilities for  $B(3, 0.5)$  and the fact that Hagar tossed the coins 200 times, to find the expected values for the number of heads.
- c** Write down the null and alternative hypotheses and the degrees of freedom for the test.

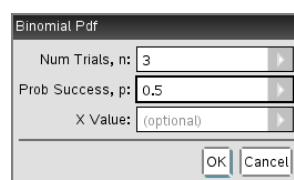
The critical value is 7.815.

Open a new document and add a Calculator page.

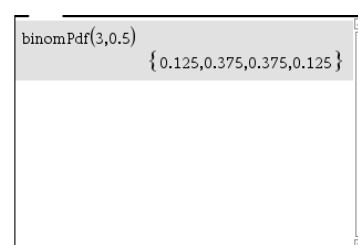
Press **menu** 5:Probability | 5:Distributions | A:Binomial Pdf...

Enter 3 as the number of trials, 0.5 as the probability of success and leave the X value empty.

Press **enter** or click OK with the touchpad.



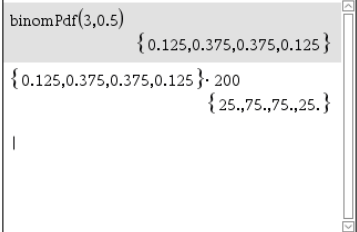
The GDC displays a list of probabilities.



## Chapter 14 / Example 14

# Goodness of fit to binomial distribution

Type  $\times 200$  and press **enter** to find the expected values.

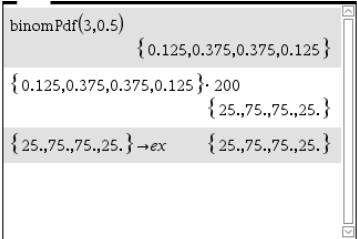


binomPdf(3,0.5)  
 $\{0.125, 0.375, 0.375, 0.125\}$   
 $\{0.125, 0.375, 0.375, 0.125\} \cdot 200$   
 $\{25., 75., 75., 25.\}$

Press **ctrl** **var** (**sto**) and type ex.

Press **enter** when you have finished.

The list you created is stored as a variable ex.

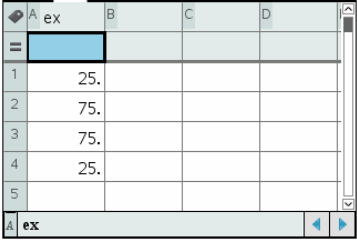


binomPdf(3,0.5)  
 $\{0.125, 0.375, 0.375, 0.125\}$   
 $\{0.125, 0.375, 0.375, 0.125\} \cdot 200$   
 $\{25., 75., 75., 25.\}$   
 $\{25., 75., 75., 25.\} \rightarrow ex$   
 $\{25., 75., 75., 25.\}$

Add a new Lists & Spreadsheet page to your document by pressing **ctrl** **doc** (**+page**) 4: Add Lists & Spreadsheet

Type 'ex' in the first cell and press **enter**.

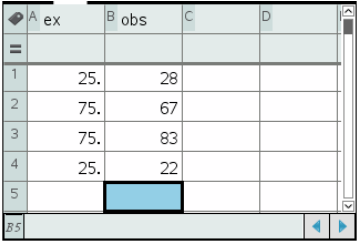
The list of expected values are displayed in the first column.



A	B	C	D
ex			
1	25.		
2	75.		
3	75.		
4	25.		
5			

Type 'obs' in the cell to the right of 'ex'

Enter the observed values in the second column.



A	B	C	D
ex	obs		
1	25.	28	
2	75.	67	
3	75.	83	
4	25.	22	
5			

To calculate the  $p$ -value

Press **menu** 4: Statistics | 4: Stat Tests | 7:  $\chi^2$  GOF...

Open the drop down lists with **►** and select using **▼** and **enter**

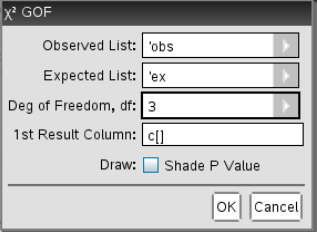
Observed List: obs

Expected List: ex

For this test you must enter the degrees of freedom yourself.

Enter df: 3

Click the touchpad on OK or press **enter**



$\chi^2$  GOF

Observed List: **obs**

Expected List: **ex**

Deg of Freedom, df: **3**

1st Result Column: **c[]**

Draw: ☐ Shade P Value

**OK** **Cancel**

Chapter 14 / **Example 14****Goodness of fit to binomial distribution**

$\chi^2 = 2.43$  and the p-value = 0.489

Either:  $2.43 < 7.815$ ,

or  $0.489 > 0.05$

Hence not significant so no reason to reject the null hypothesis.

A	ex	B	obs	C	D
=					= $\chi^2$ GOF(')
1	25.	28	Title	$\chi^2$ GOF	
2	75.	67	$\chi^2$		2.42667
3	75.	83	PVal		0.48869
4	25.	22	df		3.
5			Complis...	{0.36,0.8...	
D1 = " $\chi^2$ GOF"					